PROBLEM CORNER

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Complete solutions to this set of problems can be found at this URL:

http://140.114.32.248/d2/3problems/2014-10/Problem%20Corner.html.

You may need to install the Cabri3D plugin to view the solutions. It can be found at http://www.cabri.com/download-cabri-3d.html#plugin.

The solution to Problem 3 in Chinese can be found at:

http://pisa.math.ntnu.edu.tw/attachments/article/1075/26%20saymathsgame.pdf and its English translation at:

https://php.radford.edu/~ejmt/ProblemCornerDocs/Solution_to_Problem3_for_Oct20_14_en.pdf.

Problem 1

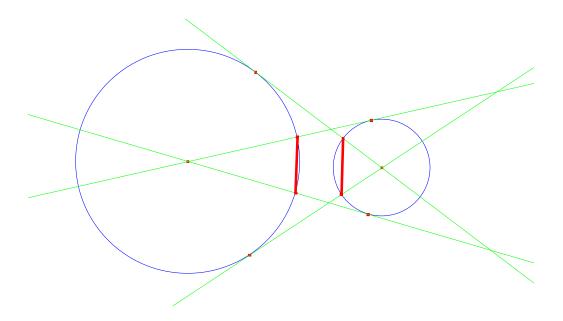
Show that the Bucky ball (truncated icosahedron) can be expressed as the intersection of an octahedron with an icosahedron.

Problem 2

In this problem, the wireframe of a cube is defined as the set formed by the union of the 12 edges. Construct three cubes so that every pair of the three wireframes meet at exact 10 points.

Problem 3

Prove the Eyeball Theorem based on expressing area of the shaded triangle (see http://sylvester.math.nthu.edu.tw/d2/3problems/2014-10/Hint.html) in two different ways.



Reference: David Well, A Dictionary of Curious and Interesting Geometry